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ON THE RELATIONSHIP BETWEEN SOME WAYS OF STOCHASTIC SYSTEMS PROGRAM CONTROL

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We call a system a stochastic system if its states change (including) under the influence of random factor. Let $\alpha(t)$ is a value of the random factor at time t . When the system program control is applied then we use forecasts of process. Let the quality of system's control in the time interval $[0, T]$ characterized by functional $\Phi(x, u, \alpha)$, where x is control function, α is a subset of the phase space of the system, which stays at the current time period is desirable. By definition, deterministic optimal control software is such a function u^* , that the functional $\Phi \stackrel{\text{def}}{=} \Phi(x^*, u^*, \alpha)$ takes the smallest value. Also by definition, stochastic optimal control is a function of u^* , which minimizes the functional $\Psi \stackrel{\text{def}}{=} E \Phi(x^*, u^*, \alpha)$, where E is the expectation operator. The question of the relationship between functionals Φ and Ψ , for example, for the possibility of (appropriate) replacement of specific cases control function on function and vice versa. It is shown that under certain quite general conditions relating to the stochastic properties of the process-difference and the possibility in the certain way approximate relationship between implementations (vector) process x and coordinates of elements of the set α functional Ψ explicitly expressed in terms of Weber functions. Each of these functions is a solution of the Cauchy problem

$$0 \leq x \leq 2^{1/2} \sqrt{\Gamma(1/2)}, \quad u \geq 0, \quad \alpha \geq 0, \quad \Gamma(1/2) = \sqrt{\pi}/2,$$

where $\Gamma(\cdot)$ - Euler gamma function, and a set of indices p is determined by the parametric of the above-mentioned approximation. It is established that when the functions are replaced in the above representation by the main part of its asymptotic at minus infinity, the functional Ψ (stochastic control) turns into the functional Φ (deterministic control). The above statements generalize some results of [1,2] concerning certain specific systems.

References

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